

Maths 4th ESO

(2.25 p)

EXAM 2_1 (FUNCTIONS/INEQUALITIES)

Name:._

1. Plot the function:
$$f(x) = \begin{cases} 2-x & \text{if } x < -1 \\ 3 & \text{if } -1 < x \le 3 \\ 2x-5 & \text{if } x > 3 \end{cases}$$
 (2p)

And find:

- a) Its domain and range.
- b) Continuity.
- c) Increasing and decreasing intervals.
- 2. Find the domain of the following functions:

f(x) =
$$\frac{x^3 + 3}{x^2 - 9x + 8}$$
; g(x) = $\sqrt[3]{\frac{x}{x^2 - 1}}$; h(x) = $\sqrt{\frac{x + 1}{9 - x^2}}$

- 3. Given the equation of the parabola $f(x) = -x^2 + 4x 3$ (1.5 p)
 - a) Find its vertex and symmetry axis.
 - b) Its intersections with the x axis and the y axis.
 - c) Draw the graph of f(x).
 - d) Find the range of f(x).

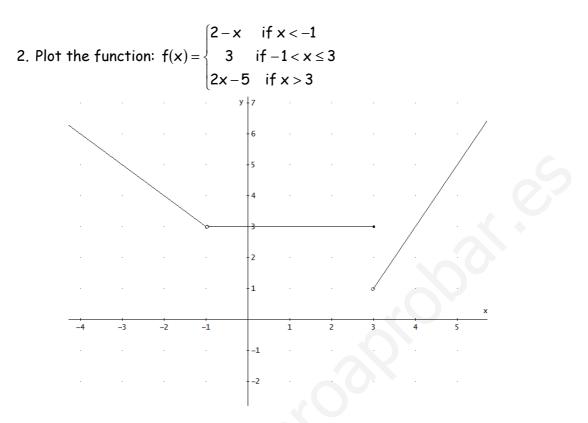
4. Solve by graphing the simultaneous equation: $\begin{array}{c} y = x^2 - 2x \\ y = x + 4 \end{array}$ (2 p)

(Write the steps you have taken to reach the solution)

- 5. Solve the following systems of inequalities: (2.25 p) b) $\frac{2(x+1) > x-7}{3} \le 2(x+1)-1$ a) $\frac{x+2y \le 10}{y > x-2}$



SOLUTION



- a) Its domain and range. $\mathsf{Dom}(f) = \mathfrak{R} - \{-1\}; \ \mathsf{Range}(f) = (1, +\infty)$
- b) Continuity. It is continuous in $(-\infty, -1) \cup (-1,3) \cup (3, +\infty)$

It has a jump discontinuity in x = 3 and a removable discontinuity in x = -1.

c) Increasing and decreasing intervals: Decreasing in $(-\infty,-1)$, Increasing in $(3,+\infty)$ and constant in (-1,3)

2. Find the domain of the following functions:

$$\begin{split} f(x) &= \frac{x^3 + 3}{x^2 - 9x + 8} \to x^2 - 9x + 8 = 0 \to x = \frac{9 \pm \sqrt{49}}{2} = \begin{cases} 8\\1 \end{cases}; \quad \text{Dom}(f) = \Re - \{1, 8\} \\ g(x) &= \sqrt[3]{\frac{x}{x^2 - 1}} \to x^2 - 1 = 0 \to x = \pm 1; \quad \text{Dom}(g) = \Re - \{1, -1\} \\ h(x) &= \sqrt{\frac{x + 1}{9 - x^2}} \to \frac{x + 1}{9 - x^2} \ge 0 \to x = -1; x = 3; x = -3, \text{ we study the sign by intervals:} \\ \text{In } (-\infty, -3) \to +; \text{ in } (-3, -1) \to -; \text{ in } (-1, 3) \to +; \text{ in } (3, +\infty) \to - \end{split}$$

So, the Domain is $Dom(h) = (-\infty, -3) \cup [-1,3)$



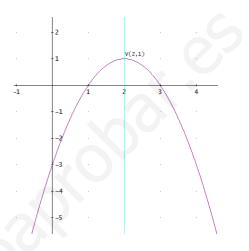
3. Given the equation of the parabola $f(x) = -x^2 + 4x - 3 \rightarrow \bigcirc$ Find its vertex and its symmetry axis

 $x = -\frac{4}{-2} = 2 \rightarrow Vertex (2, 1), symmetry axis: x = 2$

Intersections with the x-axis and the y-axis. Y-axis (0,-3)

X axis
$$-x^{2} + 4x - 3 = 0 \rightarrow x = \frac{-4 \pm \sqrt{4}}{-2} = \begin{pmatrix} 1 \\ 3 \end{pmatrix}$$

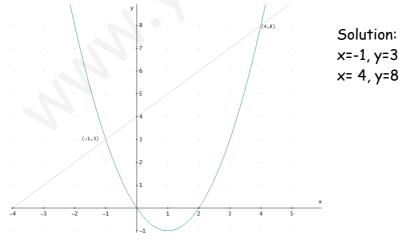
Draw the graph of f(x). Find the range of f(x). Range $(f) = (-\infty, 1]$



4. Solve by graphing the simultaneous equation: $\begin{cases} y = x^2 - 2x \\ y = x + 4 \end{cases}$

(Write the steps you have taken to reach the solution) we draw the parabola and the line: $y = x^2 - 2x \rightarrow \cup$; vertex: (1,-1)

y-intercepts \rightarrow (0,0); x-intercepts \rightarrow x² - 2x = 0 \rightarrow x(x - 2) = 0 \rightarrow $\begin{pmatrix} x = 0 \\ x = 2 \end{pmatrix}$





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