(2 p)



## EXAM 3\_3 (Geometry-Trigonometry- Probability-Surds)

1. There are two boxes. Box A contains 6 red balls and 4 blue balls and Box B contains 4 red balls and 8 blue balls. A die is rolled, if the number is less than 3, a ball is selected from box A. If the result is 3 or more, a ball is selected from Box B. Calculate:

- a) Draw a probability tree diagram to show all the outcomes the experiment.
- b) The probability that the ball will be red and selected from Box B.
- c) The probability that the ball will be blue.

2. In a classroom there are 100 pupils, of whom 40 are boys, 30 wear glasses, and 15 are boys who wear glasses. If one student from the class is randomly selected:

a) What is the probability that the student will be a girl who does not wear glasses?

b) If we know that the student selected does not wear glasses, what probability that it will be a boy? (1.5 p)

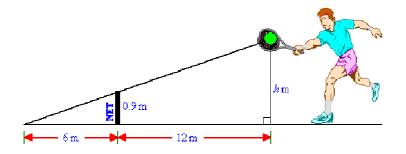
3. Calculate the height of a tree, knowing that from a point on the ground the top of the tree can be seen at an angle of  $25^{\circ}$  and from 10 m closer the top can be seen at an angle of  $52^{\circ}$ . (1.5 p)

4. a) Find the equation of the line that passes through the point (2, -3) and is perpendicular to the straight line that joins the points (4, 1) and (-2, 2). b) The line  $r \equiv 3x + ny - 7 = 0$  passes through the point A = (3, 2) and is parallel to the line  $s \equiv mx + 2y - 13 = 0$ . Calculate the values of m and n. (2 p)

5. Work out and simplify:

a) 
$$\sqrt[6]{2\sqrt[3]{2\sqrt{2}}}$$
 b)  $5\sqrt[6]{64a^2} - 5\sqrt[3]{27a} + 6\sqrt[9]{a^3}$  (1.5 p)

6. Find the value of the height, h m, in the following diagram at which the tennis ball must be hit so that it will just pass over the net and land 6 metres away from the base of the net. (1.5 p)

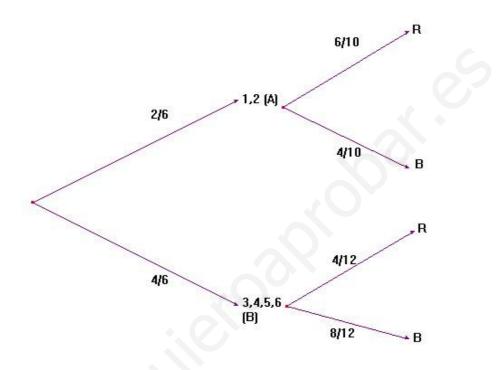




## SOLUTION

1. There are two boxes. Box A contains 6 red balls and 4 blue balls and Box B contains 4 red balls and 8 blue balls. A die is rolled, if the number is less than 3, a ball is selected from box A. If the result is 3 or more, a ball is selected from Box B. Calculate:

a) Draw a probability tree diagram to show all the outcomes the experiment.



b) The probability that the ball will be red and selected from Box B.

 $P[R \cap B] = \frac{4}{6} \cdot \frac{4}{12} = \frac{2}{9}$ 

c) The probability that the ball will be blue.

$$P[B] = \frac{2}{6} \cdot \frac{4}{10} + \frac{4}{6} \cdot \frac{8}{12} = \frac{26}{45}$$

2. In a classroom there are 100 pupils, of whom 40 are boys, 30 wear glasses, and 15 are boys who wear glasses. If one student from the class is randomly selected:

	Boys	Girls	Totals
Glasses	15	15	30
No glasses	25	45	70
Totals	40	60	100

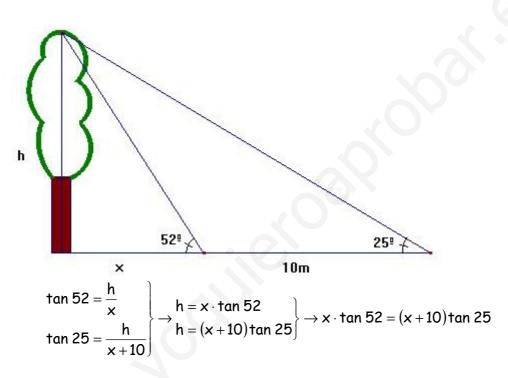
a) What is the probability that the student will be a girl who does not wear glasses?  $P[G \cap NoG] = \frac{45}{100} = 0.45$ 



b) If we know that the student selected does not wear glasses, what probability that it will be a boy?

 $P[B/N_0G] = \frac{25}{70} = \frac{5}{14}$ 

3. Calculate the height of a tree, knowing that from a point on the ground the top of the tree can be seen at an angle of 25° and from 10 m closer the top can be seen at an angle of 52°.



 $1.2799 \ x \cdot = 0.4663 \ (x + 10) \rightarrow 1.2799 \\ x - 0.4663 \\ x = 4.663 \rightarrow 0.8136 \\ x = 4.663$ 

$$x = \frac{4.663}{0.8316} = 5.73 \text{ m} \Rightarrow \text{h} = 5.73 \cdot \text{tan} 52 = 7.34 \text{ m}$$

4. a) Find the equation of the line that passes through the point (2, -3) and is perpendicular to the straight line that joins the points (4, 1) and (-2, 2). Slope of the straight line that joins (4,1) and (-2,2):  $m = \frac{2-1}{-2-4} = -\frac{1}{6} \Rightarrow \text{slope of the perpendicular line: } m = 6$ So, the equation of the line is:  $y+3 = 6(x-2) \Rightarrow y = 6x-15$ 

b) The line  $r \equiv 3x + ny - 7 = 0$  passes through the point A = (3, 2) and is parallel to the line  $s \equiv mx + 2y - 13 = 0$ . Calculate the values of m and n. 3x + ny - 7 = 0 passes through (3,2), so  $3 \cdot 3 + n \cdot 2 - 7 = 0 \rightarrow 2 + 2n = 0 \Rightarrow n = -1$ 



Maths 4<sup>th</sup> ESO

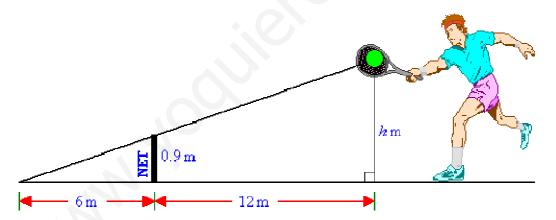
The line  $r \equiv 3x - y - 7 = 0 \rightarrow y = 3x - 7 \rightarrow \text{slope } 3$ The line  $s \equiv mx + 2y - 13 = 0 \rightarrow 2y = -mx + 13 \rightarrow y = -\frac{m}{2}x + \frac{13}{2} \rightarrow \text{slope } -\frac{m}{2}$ Parallel lines, so same slope  $\rightarrow 3 = -\frac{m}{2} \rightarrow m = -6$ 

5. Work out and simplify:

a)  $\sqrt[6]{2\sqrt[3]{2\sqrt{2}}} = \sqrt[6]{2\sqrt[3]{\sqrt{2^2 \cdot 2}}} = \sqrt[6]{2\sqrt[6]{2^3}} = \sqrt[6]{\sqrt[6]{2^6 \cdot 2^3}} = \sqrt[36]{2^9} = \sqrt[4]{2}$ 

b)  $5\sqrt[6]{64a^2} - 5\sqrt[3]{27a} + 6\sqrt[6]{a^3} = 5\sqrt[6]{2^6a^2} - 5\sqrt[3]{3^3a} + 6\sqrt[3]{a} = 10\sqrt[6]{a^2} - 15\sqrt[3]{a} + 6\sqrt[3]{a} = 10\sqrt[6]{a^2} - 15\sqrt[3]{a} + 6\sqrt[3]{a} = 10\sqrt[6]{a^2} - 15\sqrt[6]{a} = 3\sqrt[6]{a}$ 

7. Find the value of the height, h m, in the following diagram at which the tennis ball must be hit so that it will just pass over the net and land 6 metres away from the base of the net.



There are two similar triangles, because they have congruent angles. So:

 $\frac{h}{18} = \frac{0.9}{6} \Rightarrow h = \frac{0.9 \cdot 18}{6} = 2.7$  metres