

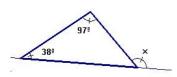
Maths 3<sup>rd</sup> ESO

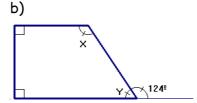
## **GEOMETRY**

1. Find the angles marked with letters

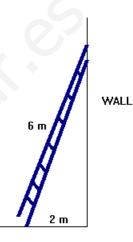
(1 point)

a)





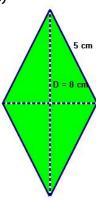
2. A ladder leans against a vertical wall. The length of the ladder is 6m. The bottom of the ladder is 2 m from the base of the wall. How high is the top of the ladder above the ground? (1 point)



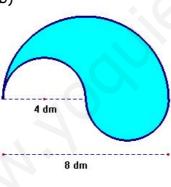
3. Find the area and perimeter of these shapes:

(3 points)

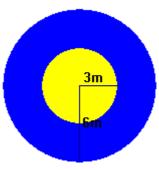
a)



b)



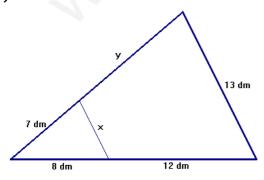
c)



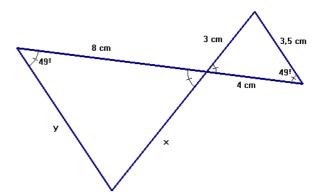
4. Use similar triangles to find the sides marked with letters:

(2 points)

a)



b)





Maths 3<sup>rd</sup> ESO

5. Work out and simplify:

$$\frac{2}{3} \!\cdot \! \left( \frac{3}{5} \!-\! \frac{1}{3} \right) \!+\! \frac{7}{5} \!\cdot \! \frac{1}{3} \!=\!$$

6. Write each of the following expressions as a single positive power: (1 point)

a) 
$$\frac{2^5 \cdot 2^4}{4 \cdot 2^3} =$$

$$b)\left(\frac{2}{5}\right)^{-2}\div\frac{5^2}{2}=$$

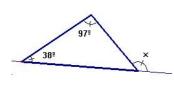
7. A television is on sale for €520. If the sale price is 20 % less than the regular price. What was the regular price? (1 point)



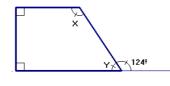
## SOLUTION

1. Find the angles marked with letters





$$97 + 38 = 135$$
  
 $\hat{X} = 135^{\circ}$ 

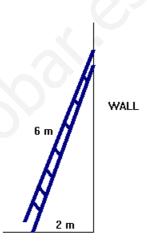


b) 
$$\hat{y} = 180 - 124 = 56^{\circ}$$
  $\hat{X} + \hat{Y} = 180$   $\hat{X} = 124^{\circ}$ 

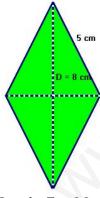
2. Right triangle: Pythagoras' Theorem

$$x^2 = 6^2 - 2^2 = 36 - 4 = 32$$

$$x = \sqrt{32} = 5.66m$$



3. Find the area and perimeter of these shapes:



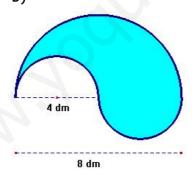
$$P=4\times 5=20~cm$$

$$A = \frac{D \cdot d}{2}$$

$$x^2 = 5^2 - 4^2 = 9$$

$$x = 3 \Rightarrow d = 6 \text{ cm}$$

$$A=\frac{8\cdot 6}{2}=24\text{ cm}^2$$



$$A = \frac{\pi \cdot r^2}{2} = \frac{\pi \cdot 4^2}{2} = 25.13 \text{ dm}^2$$

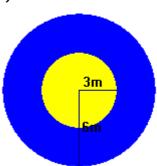
$$A = \pi \cdot 6^2 - \pi \cdot 3^2 = 84.82 \text{ m}^2$$

$$P = \text{Lcircum} + \text{LCIRCUM}$$

$$P = Lcircum + \frac{1}{2}LCIRCUM$$

$$P = 2\pi \cdot 2 + \frac{2\pi \cdot 4}{2} = 25.13 \text{ dm}$$

c)



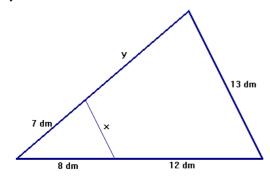
$$A = \pi \cdot 6^2 - \pi \cdot 3^2 = 84.82 \text{ m}^2$$

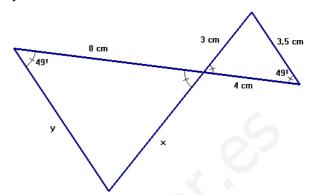
$$P = Lcircum + LCIRCUM$$

$$P=2\pi\cdot 3+2\pi\cdot 6=56.55~m$$



4. Use similar triangles to find the sides marked with letters:





$$\frac{x}{13} = \frac{8}{20} \to 20x = 104 \to x = \frac{104}{20} = 5.2 \text{ dm}$$

$$\frac{7}{z} = \frac{8}{20} \to 8z = 140 \to z = \frac{140}{8} = 17.5 \text{ dm}$$

$$z = 7 + y \to y = 17.5 - 7 \to y = 10.5 \text{ dm}$$

$$\frac{8}{4} = \frac{y}{3.5} \to 28 = 4y \to y = 7 \text{ cm}$$

$$\frac{8}{4} = \frac{x}{3} \to 24 = 4x \to x = 6 \text{ cm}$$

$$\frac{8}{4} = \frac{y}{3.5} \rightarrow 28 = 4y \rightarrow y = 7 \text{ cm}$$

$$\frac{8}{4} = \frac{x}{3} \rightarrow 24 = 4x \rightarrow x = 6 \text{ cm}$$

5. Work out and simplify:

$$\frac{2}{3} \cdot \left(\frac{3}{5} - \frac{1}{3}\right) + \frac{7}{5} \cdot \frac{1}{3} = \frac{2}{3} \cdot \frac{9 - 5}{15} + \frac{7}{15} = \frac{8}{45} + \frac{7}{15} = \frac{8}{45} + \frac{21}{45} = \frac{29}{45}$$

6. Write each of the following expressions as a single positive power:

a) 
$$\frac{2^5 \cdot 2^4}{4 \cdot 2^3} = \frac{2^5 \cdot 2^4}{2^2 \cdot 2^3} = \frac{2^9}{2^5} = 2^4$$

b) 
$$\left(\frac{2}{5}\right)^{-2} \div \frac{5^2}{2} = \frac{5^2}{2^2} \div \frac{5^2}{2} = \frac{5^2 \cdot 2}{2^2 \cdot 5^2} = \frac{1}{2}$$

7. A television is on sale for €520. If the sale price is 20 % less than the regular price. What was the regular price?

$$\frac{80}{100} = \frac{520}{x} \to 80x = 52000 \to x = \frac{52000}{80} = 650$$

The regular price was €650