

Hallar, por derivación logarítmica, la derivada de las siguientes funciones:

$$y=x^x \quad (y'=(1+\ln x) x^x)$$

$$y=x^{1/x} \quad (y'=(1-\ln x) x^{1-2/x})$$

$$y=(\operatorname{sen} x)^{\operatorname{sen} x} \quad (y'=[\cos x \ln(\operatorname{sen} x)+\cos x](\operatorname{sen} x)^{\operatorname{sen} x})$$

$$y=(\operatorname{sen} x)^{\cos x} \quad (y'=[-\operatorname{sen} x \ln(\operatorname{sen} x)+\operatorname{ctg} x \cos x](\operatorname{sen} x)^{\cos x})$$

$$y=(\operatorname{sen} x)^x \quad (y'=(\ln \operatorname{sen} x+x \operatorname{ctg} x) (\operatorname{sen} x)^x)$$

$$y=(e^x)^{\operatorname{sen} x} \quad (y'=(\operatorname{sen} x+x \cos x) e^{x \cdot \operatorname{sen} x})$$

$$y = x^{x^2} \quad (y' = (1 + 2 \ln x) x^{x^2+1})$$

$$y = (x + 1)^{x-1} \quad \left(y' = (x + 1)^{x-1} \left[\ln(x + 1) + \frac{x-1}{x+1} \right] \right)$$

$$y = (\operatorname{sen} x)^{1/x} \quad \left(y' = (\operatorname{sen} x)^{1/x} \left[\frac{-\ln \operatorname{sen} x}{x^2} + \frac{\operatorname{ctg} x}{x} \right] \right)$$

$$y = x^{\operatorname{sen} x} \quad \left(y' = \left(\cos x \cdot \ln x + \frac{\operatorname{sen} x}{x} \right) \cdot x^{\operatorname{sen} x} \right)$$