

$$\lim_{x \rightarrow +\infty} \sqrt{3x^2 + 2x + 2} - \sqrt{3x^2 + x}$$

$$\lim_{x \rightarrow 0} (\cos x)^{\left(\frac{1}{\sin x}\right)^2}$$

$$\lim_{x \rightarrow 1} \frac{\ln(2x-1)}{x^2 - \sqrt{x}}$$

$$\lim_{x \rightarrow +\infty} (\sqrt{3x^2 + 2x + 2} - \sqrt{3x^2 + x}) = (\infty - \infty) \underset{\text{Indeterminación}}{=} \lim_{x \rightarrow +\infty} \frac{(\sqrt{3x^2 + 2x + 2} - \sqrt{3x^2 + x})(\sqrt{3x^2 + 2x + 2} + \sqrt{3x^2 + x})}{\sqrt{3x^2 + 2x + 2} + \sqrt{3x^2 + x}}$$

$$= \lim_{x \rightarrow +\infty} \frac{(\sqrt{3x^2 + 2x + 2})^2 - (\sqrt{3x^2 + x})^2}{\sqrt{3x^2 + 2x + 2} + \sqrt{3x^2 + x}} = \lim_{x \rightarrow +\infty} \frac{3x^2 + 2x + 2 - (3x^2 + x)}{\sqrt{3x^2 + 2x + 2} + \sqrt{3x^2 + x}} =$$

$$= \lim_{x \rightarrow +\infty} \frac{x + 2}{\sqrt{3x^2 + 2x + 2} + \sqrt{3x^2 + x}} = \lim_{x \rightarrow +\infty} \frac{\frac{x}{x} + \frac{2}{x}}{\sqrt{\frac{3x^2}{x^2} + \frac{2x}{x^2} + \frac{2}{x^2}} + \sqrt{\frac{3x^2}{x^2} + \frac{x}{x^2}}} = \lim_{x \rightarrow +\infty} \frac{1 + 2/x}{\sqrt{3 + \frac{2}{x} + \frac{2}{x^2}} + \sqrt{3 + \frac{1}{x}}} =$$

$$= \frac{1}{\sqrt{3} + \sqrt{3}} = \boxed{\frac{1}{2\sqrt{3}}}$$

$$\lim_{x \rightarrow 0} (\cos x)^{\left(\frac{1}{\sin x}\right)^2} = \cos 0^{\left(\frac{1}{\sin 0}\right)^2} = (1^\infty) \quad (*) = e^{\lim_{x \rightarrow 0} \left(\frac{1}{\sin x}\right)^2 (\cos x - 1)}$$

INDETERMINACION

$$= e^{\lim_{x \rightarrow 0} \frac{\cos x - 1}{\sin^2 x}} = e^{\frac{0}{0}} \stackrel{\text{L'Hopital}}{=} e^{\lim_{x \rightarrow 0} \frac{-\sin x}{2 \sin x \cos x}} = e^{\lim_{x \rightarrow 0} \frac{-1}{2 \cos x}} = e^{-1/2} = \boxed{\frac{1}{\sqrt{e}}}$$

(*) UTILIZAMOS $\lim_{x \rightarrow a} f(x)^{g(x)} = e^{\lim_{x \rightarrow a} g(x) [f(x) - 1]}$

$$\lim_{x \rightarrow 1} \frac{\ln(2x-1)}{x^2 - \sqrt{x}} = \frac{\ln(2 \cdot 1 - 1)}{1^2 - \sqrt{1}} = \left(\frac{0}{0}\right) \stackrel{\text{L'Hopital}}{=} \lim_{x \rightarrow 1} \frac{\frac{1}{2x-1} \cdot 2}{2x - \frac{1}{2\sqrt{x}}} = \frac{\frac{2}{1}}{2 - \frac{1}{2}} = \frac{2}{3/2} = \boxed{\frac{4}{3}}$$